

Permutation of Dynamically Sized Array

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Simple things should be simple...

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Input :

- $X1 = [11,22,33]$
- $X2 = [44,55]$

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- $X1 = [11,22,33]$
- $X2 = [44,55]$

Output

- $(11,44) ;(11,55);(22,44);(22,55);(33,44);(33,55)$

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Not infinity just

unknown or dynamic

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The Clock...

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- 10:58:59 am
10:59:00 am

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We can use the same concept to make permutations

- $X = X_1 + X_2 + \dots$
- L = saving lower limits
- U = saving upper limits

Example

- $X1 = [10, 20, 30]$ $X2 = [40, 50]$
 $X3 = [60, 70, 80]$

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 $X3 = [60,70,80]$
- $X = X1 + X2 + X3$
 $X = [10,20,30,40,50,60,70,80]$
- $L = [1,4,6]$
- $U = [3,5,8]$

Algorithm

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 $[2,4,6]$
 $[2,4,7]$
 :
 $I = U$